

1A) Calculate C that gives resonance frequency $f_0 = 50 \text{ kHz}$

$$f_0 = \frac{\omega_0}{2\pi} = \frac{1}{2\pi\sqrt{LC}} \text{ in Hz}$$

$$50 \text{ kHz} = \frac{1}{2\pi\sqrt{10 \times 10^{-3} C}}$$

$$50 \times 10^3 (2\pi\sqrt{10 \times 10^{-3}}) = \frac{1}{\sqrt{C}}$$

$$\frac{1}{50 \times 10^3 (2\pi \times 10^{-1})} = \sqrt{C}$$

$$C = 1.01 \times 10^{-9} \approx 1 \text{ nF}$$

1B) $f_d = \omega_d / 2\pi$ J is constant for $R_1 = 0$, $R_1 = 100$ and $1 \text{ k}\Omega$.

$$\omega_d = \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}, \text{ At } R_1 = 0 \text{ } R_{\text{total}} = 250 \text{ ohm}$$

$$\omega_{d1} = \sqrt{10^{11} - \frac{(250)^2 \times 10^4}{4}} = 3.15 \times 10^5, f_{d1} = 50 \times 10^3 = 50 \text{ kHz}$$

$$R = 100$$

$$\omega_{d2} = \sqrt{10^{11} - \frac{(1250)^2 \times 10^4}{4}} = 3.15 \times 10^5, f_{d1} = 50 \times 10^3 = 50 \text{ kHz}$$

$$R = 1 \text{ k}\Omega$$

$$\omega_{d3} = \sqrt{10^{11} - \frac{(12500)^2 \times 10^4}{4}} = 3.1 \times 10^5 f_{d1} = 49 \times 10^3 = 49 \text{ kHz}$$

1C

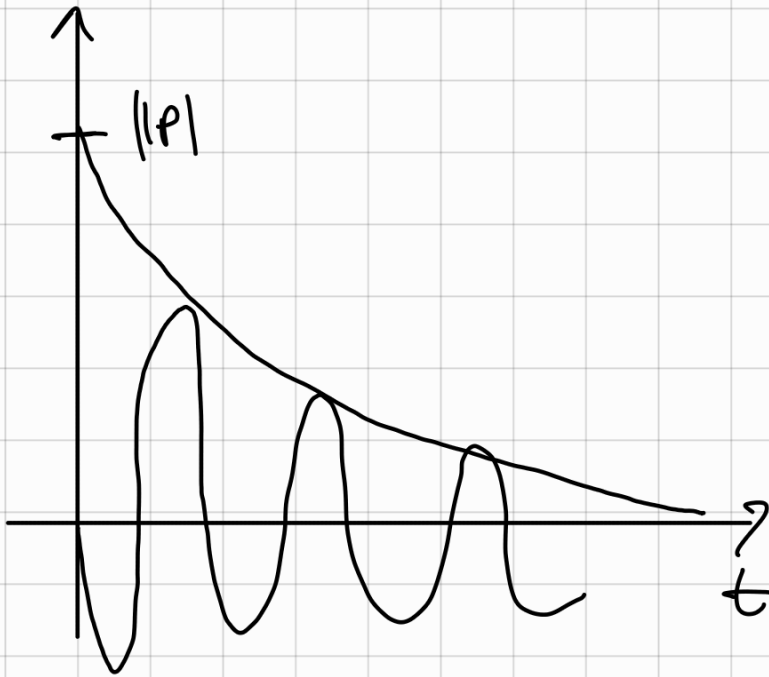
$$i(t) = I_P \sin(\omega_d t) e^{-t/J}$$

$$V_C(0^-) = V_{in} = 5 \text{ V}$$

$$i(0^-) = i(0^+) = 0 \quad I_P = \frac{-1}{\omega_d} \frac{V_C(0)}{L} = \frac{-1}{3.15 \times 10^5} \frac{5}{10^{-2}} = \frac{-5}{3.15 \times 10^3}$$

$$|p| = -1,58 \times 10^{-3}, \quad ||p| = 1,58 \times 10^{-3} \quad \gamma = \frac{2 \cdot 10^{-2}}{35} = \frac{0,02}{35} = 5,71 \times 10^{-5}$$

$$i(t) = -1,58 \times 10^{-3} \sin(3,15 \times 10^5 t) e^{-t/5,71 \times 10^{-5}}$$



$$v_c = C \frac{dQ}{dt}$$

$$Q = \int_0^t i(t) dt + i_0$$

$$\hookrightarrow v_c(t) = \int_0^t i(t) = -1,58 \times 10^{-3} \sin(3,15 \times 10^5 t) e^{-t/5,71 \times 10^{-5}}$$

$$1) R = 2 \sqrt{\frac{L}{C}} = 6293,16$$

$$2) R_1 = 0 \Omega \quad V_{LC} = i(t) \cdot 200 = 2V$$

$$i(t) = \frac{2,5 \sin(\omega t)}{250 + R_1}$$

$$R_1 = 100 \Omega$$

$$i(t) = \frac{2,5}{350} = 0,00714 \quad , \quad V_C(t) = \frac{L (2,5) \omega \cos(\omega t)}{350} = 1,4V$$

$$R_1 \neq 0 = 1 \Omega$$

$$i(t) = 0,002$$

$$V_C(t) = \frac{L \cdot 2,5 \cdot \omega \cdot \cos(\omega t)}{1250} = 0,4$$

$$J = 1,6 \times 10^{-5}$$

$$V_C(t) = \frac{-1}{\omega_d R C} V_p \cos(\omega_d t) \text{ when } \omega_d \sqrt{\frac{1}{LC} - \frac{R^2}{4L}}$$

Case 1 $10L_1$ and $0.1C_1$

Case 2 $0.1L_1$ and C_1

at $t=0$ V_p are equal $\rightarrow 5V$ so we need to

look $\frac{-1}{\omega_d R C}$ value so this a negative value

so if we want bigger values we must increase

$\omega_d \cdot R \cdot C$ values R is equal for both cases

for ω_d there is no big difference at all but C

values makes the difference so $\text{Case 2 } |V(t)| > \text{Case 1 } |V(t)|$